

Projective indecomposable modules are classical objects of study in the modular representation theory of finite groups. However, surprisingly little is known about their dimensions. There is some progress in computing minimum dimensions of them for finite simple groups. This will be described in the talk, and some promising problems for further research in the area will be suggested.